

Energy Efficient Variable Stiffness Actuators

Conceptual Design and Implementation

Ludo C. Visser, Raffaella Carloni and Stefano Stramigioli

Department of Electrical Engineering
University of Twente, The Netherlands

Motivation

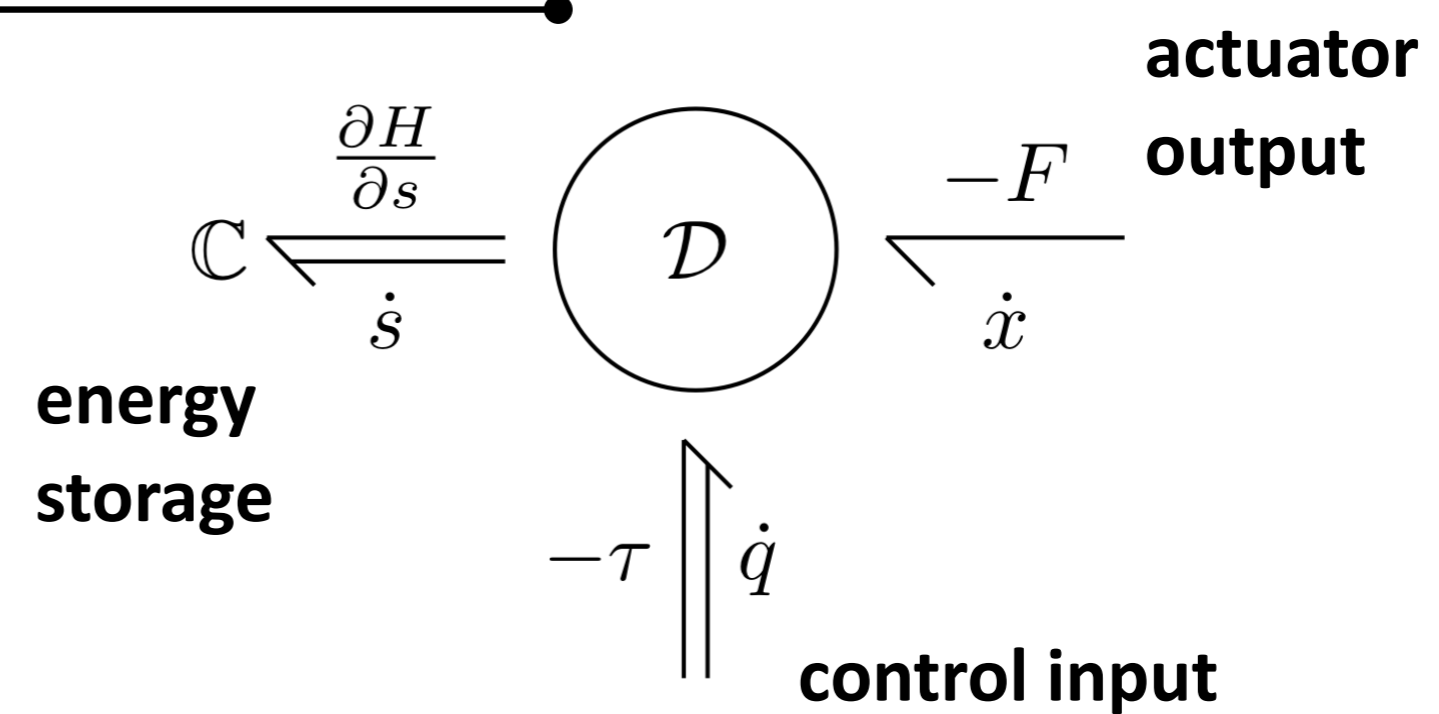
Variable stiffness actuators have internal degrees of freedom and internal springs:

- + the degrees of freedom are used to change the **apparent output stiffness**;
- + the apparent output stiffness can be changed independently of the output position;
- + the springs can be used to store **energy**;
- + the **configuration** of the degrees of freedom determines **power flow** between the **springs** and the **output**.

Goal:

Change the output stiffness without changing the energy stored in the springs.

Port-based Modeling



The Dirac structure \mathcal{D} defines the power flows among the bonds:

$$\begin{bmatrix} \dot{s} \\ \tau \\ F \end{bmatrix} = \underbrace{\begin{bmatrix} 0 & A(q, x) & B(q, x) \\ -A^T(q, x) & 0 & 0 \\ -B^T(q, x) & 0 & 0 \end{bmatrix}}_{\mathcal{D}} \begin{bmatrix} \frac{\partial H}{\partial s} \\ \dot{q} \\ \dot{x} \end{bmatrix}$$

Variation of the energy in the spring:

$$\frac{dH}{dt} = \frac{\partial H}{\partial s} (A(q, x)\dot{q} + B(q, x)\dot{x})$$

Conceptual Design

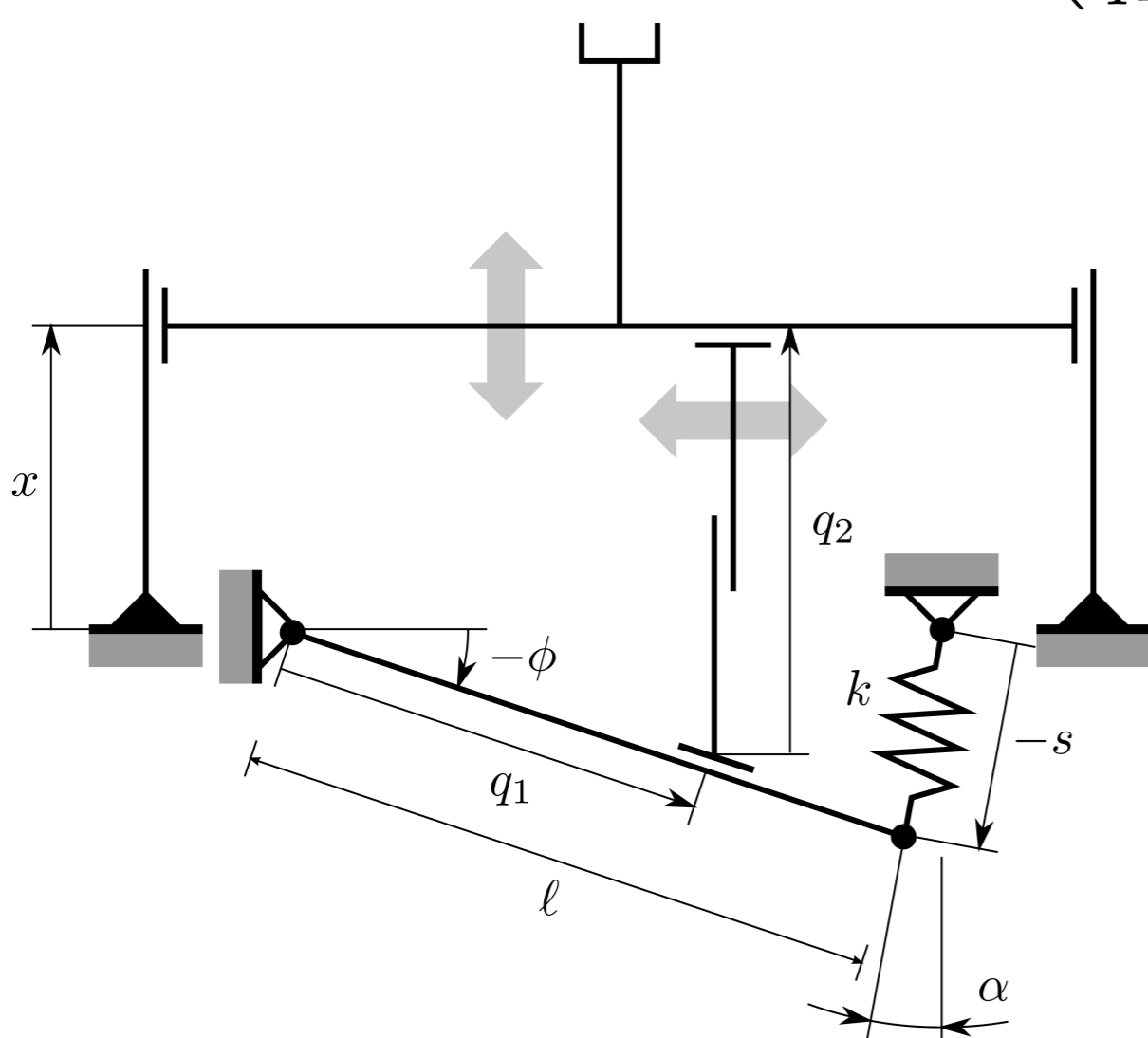
The energy in the spring changes with **no power flow via the control port** if:

$$\dot{q} \in \ker A(q, x), \quad \forall q, x$$

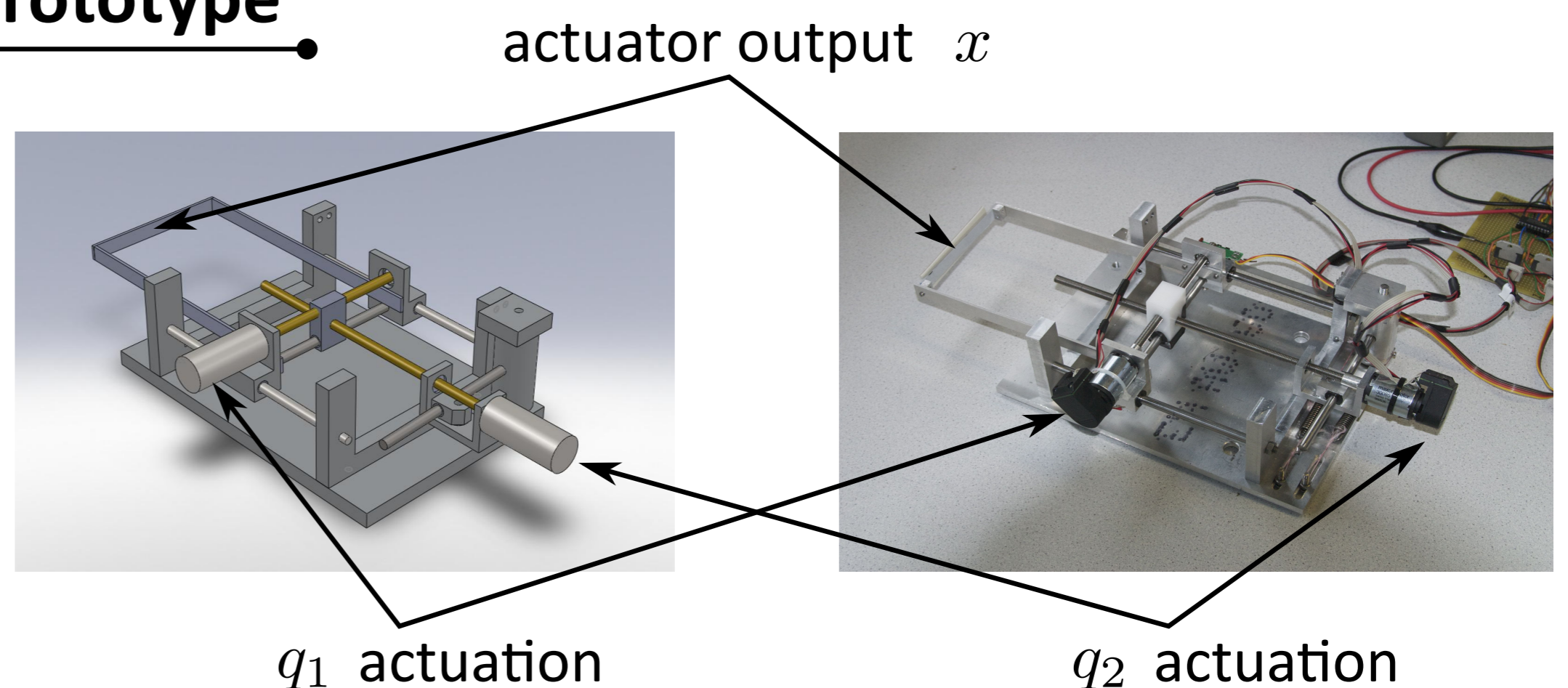
The conceptual design has:

$$A(q, x) = \frac{\ell}{q_1} \begin{bmatrix} \sin \phi & 1 \end{bmatrix}$$

The output stiffness is: $K := \frac{\partial F}{\partial x} = \left(\frac{\ell}{q_1}\right)^2 k$



Prototype



- + Output **position** and **stiffness** are mechanically **decoupled**.
- + The **output stiffness** can be changed **without changing the energy stored** in the springs.

